

**Perpendicular Amplitude  
Correction Coefficients for  
1,3-Butadiene from Spectroscopic  
Data**

S. J. CYVIN

*Institutt for teoretisk kjemi, Norges tekniske  
høgskole, Trondheim, Norway*

and

M. TRÆTTEBERG and G. HAGEN

*Kjemisk institutt, Norges lærerhøgskole,  
Trondheim, Norway*

**R**ecently the mean amplitudes of vibration<sup>1</sup> ( $u$ ) for 1,3-butadiene have been calculated from spectroscopic data<sup>2</sup> and compared with electron diffraction values. The similar work<sup>3</sup> on *cis* and *trans* 1,3,5-

**Table 1.** 1,3-Butadiene: Calculated perpendicular amplitude correction coefficients (Å units).

Distance	(equil.)	T = 0	298°K
C <sub>1</sub> —H <sub>1</sub>	(1.094)	0.0179	0.0198
C <sub>1</sub> —H <sub>1'</sub>	(1.094)	0.0219	0.0288
C <sub>2</sub> —H <sub>2</sub>	(1.094)	0.0168	0.0204
C <sub>1</sub> =C <sub>2</sub>	(1.344)	0.0036	0.0065
C <sub>2</sub> —C <sub>3</sub>	(1.467)	0.0014	0.0015
C <sub>1</sub> ···C <sub>3</sub>	(2.469)	0.0017	0.0032
C <sub>1</sub> ···C <sub>4</sub>	(3.695)	0.0002	0.0002
C <sub>2</sub> ···H <sub>1</sub>	(2.110)	0.0104	0.0131
C <sub>2</sub> ···H <sub>1'</sub>	(2.110)	0.0135	0.0228
C <sub>1</sub> ···H <sub>2</sub>	(2.110)	0.0106	0.0173
C <sub>2</sub> ···H <sub>3</sub>	(2.201)	0.0074	0.0093
C <sub>3</sub> ···H <sub>1</sub>	(3.456)	0.0059	0.0075
C <sub>3</sub> ···H <sub>1'</sub>	(2.692)	0.0096	0.0165
C <sub>1</sub> ···H <sub>3</sub>	(2.709)	0.0075	0.0127
C <sub>1</sub> ···H <sub>4</sub>	(4.577)	0.0034	0.0038
C <sub>1</sub> ···H <sub>4'</sub>	(4.031)	0.0042	0.0058
H <sub>1</sub> ···H <sub>1'</sub>	(1.905)	0.0247	0.0320
H <sub>1</sub> ···H <sub>2</sub>	(2.422)	0.0151	0.0209
H <sub>1'</sub> ···H <sub>2</sub>	(3.081)	0.0155	0.0277
H <sub>2</sub> ···H <sub>3</sub>	(3.151)	0.0087	0.0092
H <sub>1</sub> ···H <sub>3</sub>	(3.798)	0.0094	0.0131
H <sub>1</sub> ···H <sub>3'</sub>	(2.469)	0.0185	0.0331
H <sub>1</sub> ···H <sub>4</sub>	(5.536)	0.0050	0.0052
H <sub>1'</sub> ···H <sub>4</sub>	(4.724)	0.0071	0.0091
H <sub>1'</sub> ···H <sub>4'</sub>	(4.610)	0.0054	0.0058

hexatriene also includes the calculated perpendicular amplitude correction coefficients<sup>1</sup> ( $K$ ). These quantities are (in common with the mean amplitudes) of great interest in modern interpretations of gas electron diffraction measurements. In Table 1 the calculated results of  $K$  values for 1,3-butadiene are presented. They were obtained from the harmonic force field previously used in the mean amplitude calculations.<sup>2</sup> The interatomic distances are given (see Table 1) in the same sequence as in Table 2 of the cited work,<sup>2</sup> and approximate equilibrium separations ( $r_e$  in Å units) are included in parentheses.

It is intended to use these  $K$  values along with those of hexatrienes<sup>2</sup> in refined structure studies of hydrocarbons with conjugated double bonds in connection with the systematic electron diffraction investigations of such molecules.<sup>4</sup> When the  $K$  values are known it is possible to derive the average structure<sup>5</sup> with the aid of the relation

$$r_a = r_g(1) + (u^2/r_e) - K \quad (1)$$

The angles  $\theta\alpha$  of the average structure may be determined from the bonded and nonbonded  $r_a$  distances by Euclidean geometry. Thus the incorporation of  $K$  values according to eqn. (1) into a least-squares refinement of electron diffraction measurements should theoretically improve the exploitation of the material in a rational way.

1. Cyvin, S. J. *Molecular Vibrations and Mean Square Amplitudes*, Universitetsforlaget, Oslo, and Elsevier, Amsterdam 1968.
2. Trætteberg, M., Hagen, G. and Cyvin, S. J. *Acta Chem. Scand.* **23** (1969) 74.
3. Cyvin, S. J., Hagen, G. and Trætteberg, M. *Acta Chem. Scand.* **23** (1969). *In press*.
4. Haugen, W. and Trætteberg, M. In Andersen, P., Bastiansen, O. and Furberg, S. *Selected Topics in Structure Chemistry*, Universitetsforlaget, Oslo 1967, p. 113; Trætteberg, M. *Acta Chem. Scand.* **22** (1968) 628, 2294, 2305.
5. Morino, Y., Kuchitsu, K. and Oka, T. J. *Chem. Phys.* **36** (1962) 1108; Kuchitsu, K. and Konaka, S. *J. Chem. Phys.* **45** (1966) 4342.

Received April 15, 1969.